

7.4 Warm-Up

$y = mx + b$
 $Ax + By + C = 0$
 $y - y_1 = m(x - x_1)$

change to slope $y = mx + b$ intercept

1. Identify the slope of each linear equation.

a) $3x - y + 8 = 0$

$3x + 8 = y$ $m = 3$

b) $2x - 5y + 7 = 0$

$-2x - 7 = -5y$
 $\frac{-5y}{-5} = \frac{-2x - 7}{-5}$
 $y = \frac{2}{5}x + \frac{7}{5}$ $m = \frac{2}{5}$

2. Write the equation of each line in slope-point form.

a) slope of $\frac{2}{3}$ and passing through $(-1, 5)$

$y - 5 = \frac{2}{3}(x - (-1))$
 $y - 5 = \frac{2}{3}(x + 1)$

b) passing through $(4, 2)$ and $(8, 3)$

$y - 2 = \frac{1}{4}(x - 4)$
 $y - 3 = \frac{1}{4}(x - 8)$
 $m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{2 - 3}{4 - 8} = \frac{-1}{-4} = \frac{1}{4}$

3. Write the equation of each line in slope-intercept form.

a) slope of -4 and passing through $(2, 7)$

$y - 7 = -4(x - 2)$
 $y - 7 = -4x + 8$
 $+7$ $+7$
 $y = -4x + 15$

b) passing through $(2, 5)$ and $(0, 6)$

$y - 6 = -\frac{1}{2}(x - 0)$
 $y - 6 = -\frac{1}{2}x$
 $y = -\frac{1}{2}x + 6$
 $m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{5 - 6}{2 - 0} = \frac{-1}{2}$

4. Write an equation in general form of the line that passes through $(3, 7)$ and $(5, -1)$.

$y - 7 = -4(x - 3)$
 $y - 7 = -4x + 12$
 $y = -4x + 19$
 $0 = -4x - y + 19$
 $m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{7 - (-1)}{3 - 5} = \frac{8}{-2} = -4$

5. Complete each statement.

a) $\frac{2}{3}$ is to $-\frac{3}{2}$ as $\frac{4}{5}$ is to \square . $-\frac{5}{4}$ b) -4 is to $\frac{1}{4}$ as -3 is to \square . $\frac{1}{3}$ c) $\frac{1}{2}$ is to -2 as $-\frac{1}{5}$ is to \square . 5

parallel lines have equal slopes

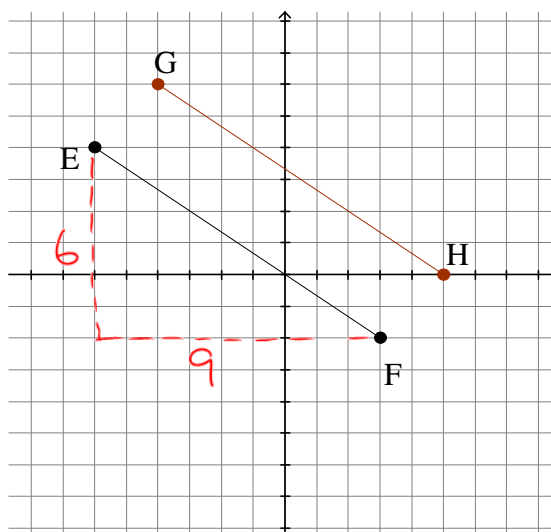
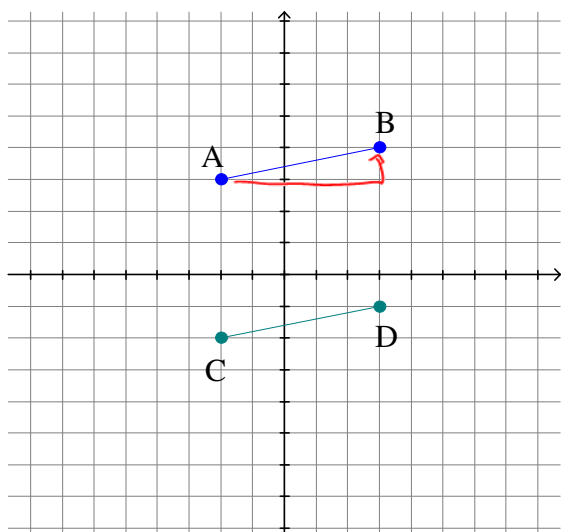
perpendicular lines are opposite AND reciprocal

7.4 Parallel and Perpendicular Lines

Objectives:

- Relate the slopes of parallel lines
- Relate the slopes of perpendicular lines
- Solve problems using parallel and perpendicular lines

Find the slopes of each of the line segments below.



$$m_{AB} = \frac{1}{5}$$

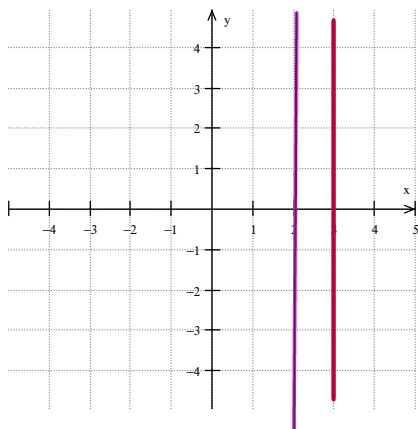
$$m_{CD} = \frac{1}{5}$$

$$m_{EF} = -\frac{2}{3}$$

$$m_{GH} = -\frac{2}{3}$$

What do you notice about the slopes of parallel lines?

Parallel Lines: have the same slope
and
2 lines with the same slope are parallel



The line shown has a slope of n.p.

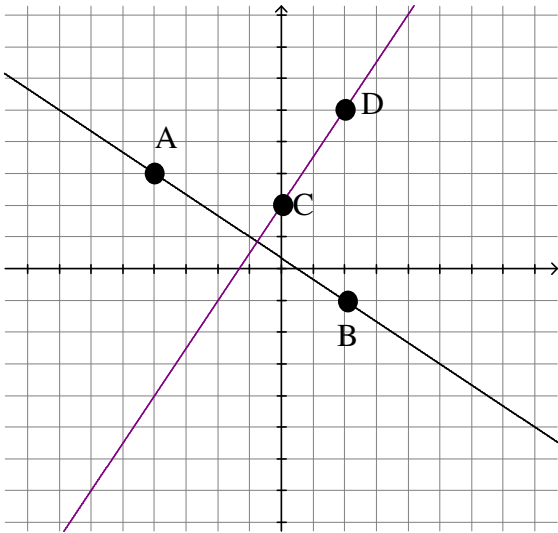
Draw a parallel line on the same grid. What is the slope of the parallel line?

slope of parallel line = n.p.

$$x=2$$

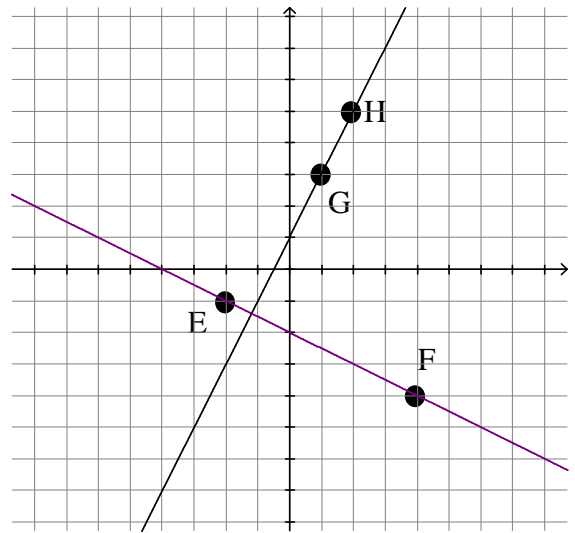
$$x=3$$

Find the slopes of each of the following pairs of perpendicular lines. **Write all answers as fractions in lowest terms:**



$$m_{AB} = -\frac{2}{3}$$

$$m_{CD} = \frac{3}{2}$$



$$m_{EF} = -\frac{1}{2}$$

$$m_{GH} = \frac{2}{1}$$

Perpendicular Lines: have slopes that are opposites and reciprocals

$m = \frac{2}{7}$ and $-\frac{7}{2}$ are perpendicular

Draw the line given by the equation:

$$3x + 6y - 12 = 0.$$

$$\begin{array}{c|c} x & y \\ \hline 0 & 2 \\ 4 & 0 \end{array}$$

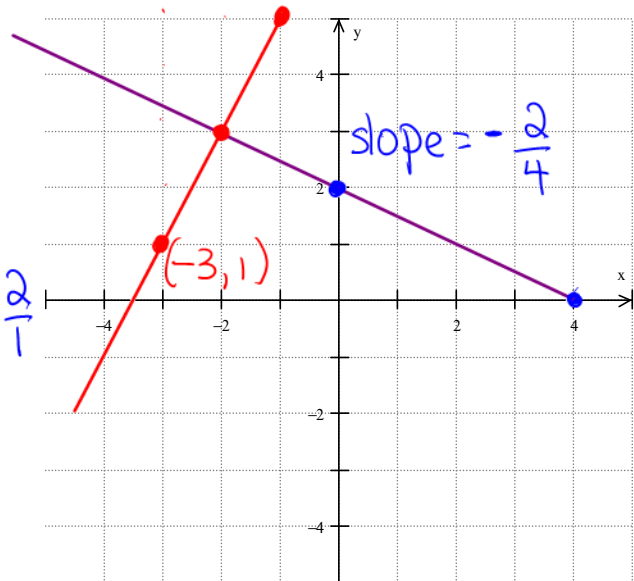
Draw the perpendicular line that passes through (-3,1) and find its equation.

perpendicular slope = $\frac{4}{2}$ or $\frac{2}{1}$

point slope

$$y - k = m(x - h)$$

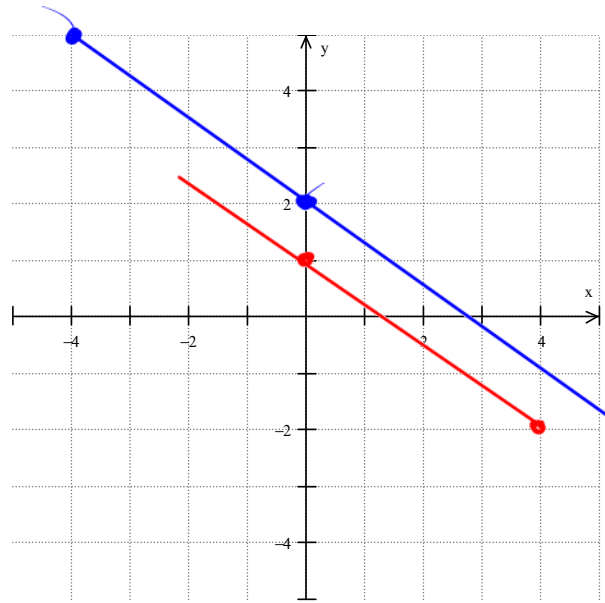
$$y - 1 = \frac{2}{1}(x + 3)$$



Draw the lines given by the equations:

$$\begin{aligned}
 3x + 4y - 8 &= 0 \\
 -4y &= -3x + 8 \\
 4y &= 3x - 8 \\
 y &= \frac{3}{4}x - 2
 \end{aligned}$$

$$\begin{aligned}
 6x + 8y - 8 &= 0 \\
 -8y &= -6x + 8 \\
 8y &= 6x - 8 \\
 y &= \frac{3}{4}x - 1
 \end{aligned}$$



The lines are parallel because:

$$\begin{aligned}
 -\frac{6}{8}x + 1 &= y \\
 \boxed{y = -\frac{3}{4}x + 1}
 \end{aligned}$$

they have the same slope

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Find the equation of a perpendicular line to $3x + 4y - 6 = 0$

Some different methods you could try include:

① need to find the slope

$$m = \frac{4}{3}$$

$$y = \frac{4}{3}x + \square$$

find slope

$$\begin{aligned}
 3x + 4y - 6 &= 0 \\
 -4y &= -3x + 6 \\
 4y &= 3x - 6 \\
 y &= \frac{3}{4}x - \frac{3}{2}
 \end{aligned}$$

Three coordinates A(-1,-1), B(3,-2) and C(4,3) form a triangle. Is this a right triangle?

no. in order for angle B to be a 90° angle, the slope of AB must be perpendicular to slope of BC.

They are not perpendicular because they are not opposite and reciprocal.

