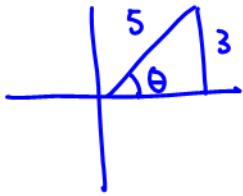


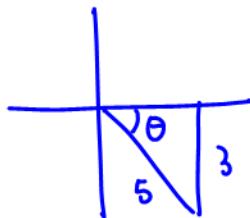
Inverse Trigonometric Functions

1. Draw and label diagrams showing the following angles:

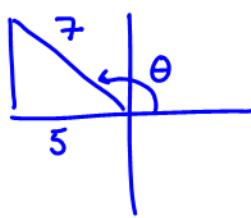
a) $\sin^{-1}\left(\frac{3}{5}\right)$



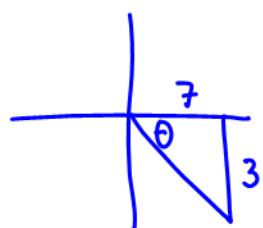
b) $\sin^{-1}\left(-\frac{3}{5}\right)$



c) $\cos^{-1}\left(-\frac{5}{7}\right)$

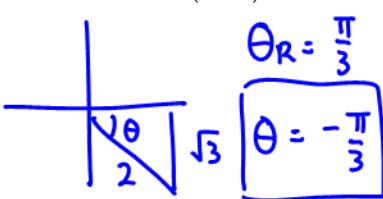


d) $\tan^{-1}\left(-\frac{3}{7}\right)$

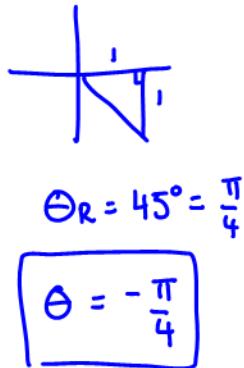


2. Determine the following:

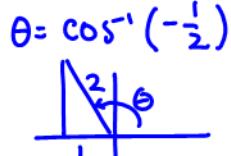
a) $\theta = \sin^{-1}\left(-\frac{\sqrt{3}}{2}\right)$



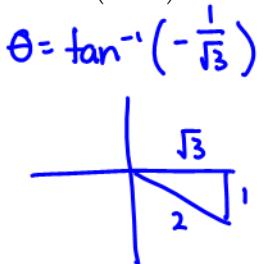
b) $\theta = \arctan(-1)$



c) $\sec^{-1}(-2)$

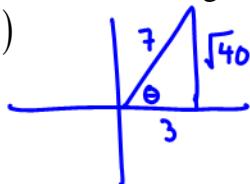


d) $\operatorname{arc cot}\left(-\sqrt{3}\right)$



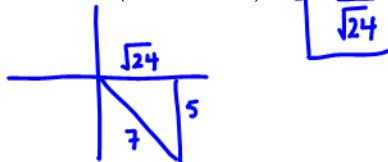
3. Determine the following:

a) $\sin(\cos^{-1}\frac{3}{7})$

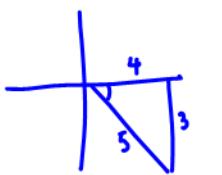


$$\sin(\cos^{-1}\frac{3}{7}) = +\frac{\sqrt{40}}{7}$$

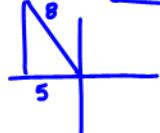
b) $\tan(\sin^{-1}\left(-\frac{5}{7}\right))$



c) $\cos(\sin^{-1}\left(-\frac{3}{5}\right))$



d) $\cos(\cos^{-1}\left(-\frac{5}{8}\right)) = -\frac{5}{8}$



e) $\tan(\sin^{-1} x)$

$$\begin{aligned}\frac{x^2}{1} + \frac{\sqrt{1-x^2}^2}{1} &= 1 \\ \sqrt{1-x^2}^2 &= 1 - x^2 \\ \sqrt{1-x^2} &= \sqrt{1-x^2}\end{aligned}$$

$$\tan(\sin^{-1} x) = \frac{x}{\sqrt{1-x^2}}$$

g) $\cos(\sin^{-1} x)$
uses same diagram as "e"

$$\cos(\sin^{-1} x) = \frac{\sqrt{1-x^2}}{1} \text{ or } \sqrt{1-x^2}$$

f) $\sin(\sin^{-1} x)$
uses same diagram as "e"

$$\sin(\sin^{-1} x) = x$$

g) $\csc(\cos^{-1} x)$

$$\csc \theta = \frac{1}{\sin \theta}$$

$$\csc(\cos^{-1} x) = \frac{1}{\sqrt{1-x^2}}$$

4. Evaluate the following:

a) $\sin^{-1}(\sin \frac{2\pi}{3})$

$$\sin \frac{2\pi}{3} = \frac{\sqrt{3}}{2}$$

$\sin^{-1}(\frac{\sqrt{3}}{2})$

$$\boxed{\theta = \frac{\pi}{3}}$$

b) $\sin^{-1}(\sin \frac{\pi}{3})$

$$\sin \frac{\pi}{3} = \frac{\sqrt{3}}{2}$$

$\sin^{-1}(\frac{\sqrt{3}}{2})$ same diagram as above

$$\sin^{-1}(\sin \frac{\pi}{3}) = \frac{\pi}{3}$$

c) $\cos^{-1}(\sin \frac{11\pi}{6})$

$$\sin \frac{11\pi}{6} = -\frac{1}{2}$$

$\cos^{-1}(-\frac{1}{2})$

$$\theta_R = \frac{\pi}{3}$$

$$\boxed{\theta = \frac{2\pi}{3}}$$

d) $\arctan(\cot \frac{4\pi}{3})$

$$\cot \frac{4\pi}{3} = \frac{1}{\sqrt{3}}$$

$\tan^{-1}(\frac{1}{\sqrt{3}}) = \frac{\pi}{6}$

$\theta_R = \frac{\pi}{6}$

$$\boxed{\theta = \frac{\pi}{6}}$$

5. For what values of x are the following statements true?

a) $\sin(\sin^{-1} x) = x$

always true because $\sin^{-1}(x)$ will always make $-\frac{\pi}{2} \leq \theta \leq \frac{\pi}{2}$

$$\sin^{-1}(\sin \theta) = \theta$$

b) $\sin^{-1}(\sin x) = x$

only true if $-\frac{\pi}{2} \leq x \leq \frac{\pi}{2}$

because x represents the angle in this case.