

## 6.2 Linear Relations

Recall that a relation is an association between two quantities. A **linear relation** will have a graph that is a line. A **non-linear relation** will have a graph that is some type of curve. To determine if a relation is linear from a table of values, check to see how the x and y values are related. If the x and y values increase or decrease by a constant amount, then the data would be for a linear relation (except for horizontal or vertical lines). Non-linear relations would have x and y values that increase or decrease by different amounts.

Example:

linear relations have a constant rate

### Linear Relation

x	y
1	8
2	12
3	16
4	20
5	24

+1  
+1

+4  
+4

rate =  $\frac{4}{1}$   
rate =  $\frac{4}{1}$

constant rate =  $\frac{4}{1}$

Equation:

$$y = 4 \cdot x + 4$$

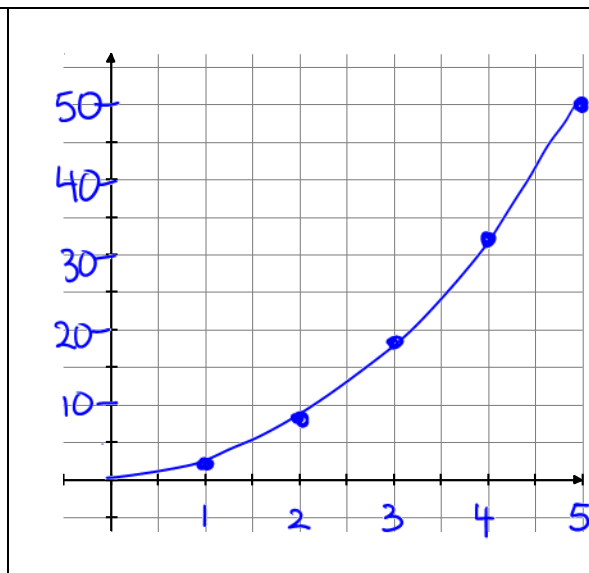
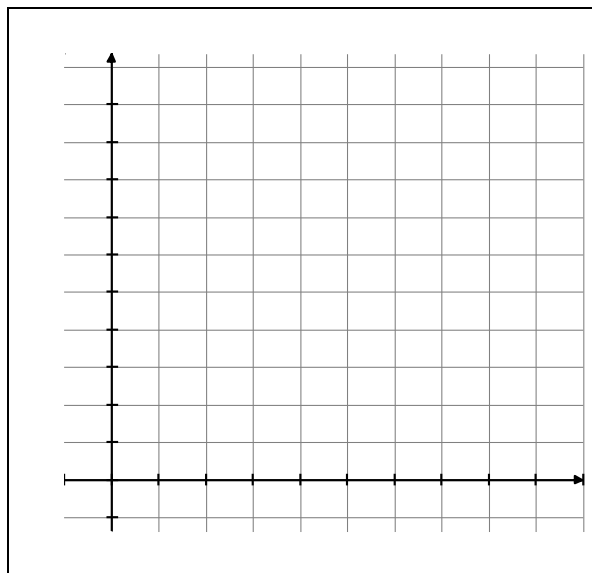
### Non-Linear Relation

x	y
1	2
2	8
3	18
4	32
5	50

> rate =  $\frac{6}{1}$   
> rate =  $\frac{10}{1}$

Equation:  $y = 2x^2$

non linear  
 $y = x^2$   
 $y = \sqrt{x}$



Graphs of linear relations may contain one of two different types of data:

Discrete Data: disconnected data, certain numbers cannot be placed on graph  
eg amounts of donuts

Continuous Data:

connected data: you can have amounts between coordinates

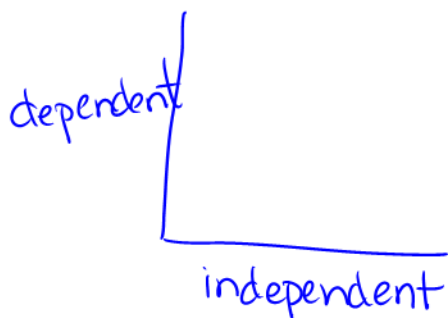
For what type of situation would you see each type of data?

discrete - you only have whole number amounts

continuous - weights/heights may have decimals

In relations that contain two variables, one variable is considered to be **independent** while the other is considered to be **dependent**. As would be expected, the dependent variable's values depend on the values of the independent variable.

- When data is presented in tabular form, the independent values are found in the first column and the dependent values are found in the second column.
- When data is presented in graph form, the independent values are on the x-axis (horizontal) and the dependent values are on the y-axis (vertical).

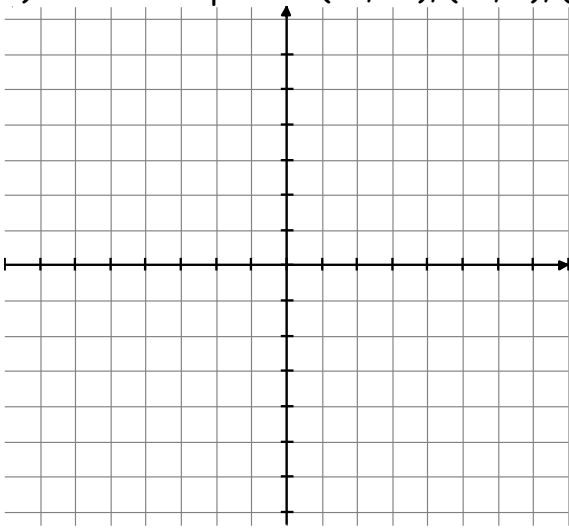


in rates, the rate is always # dependent per # independent.

Examples:

1) For each of the following groups of data, determine whether or not they represent a linear relation.

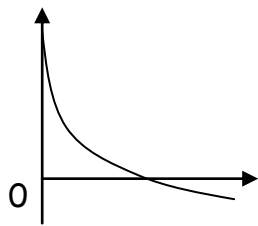
a) The set of points:  $(-7, 10)$ ,  $(-4, 8)$ ,  $(-1, 6)$ ,  $(2, 4)$ ,  $(5, 2)$ ...



can determine if linear  
by  
a) determining if  
constant rate  
b) plotting

|| |

b) The graph below shows the radioactive decay of an isotope in a sample of rock.

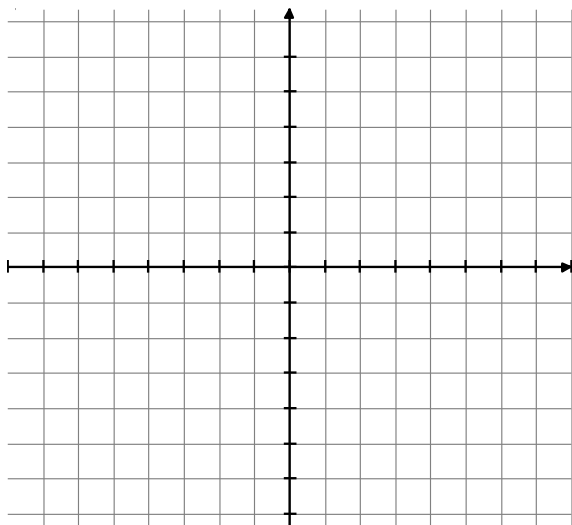


Amount vs. Time

↑ dependent ↑ independent.

p 287 # 1-10 \* 11, \* 12

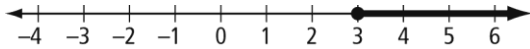
c) The relation described by the following equation:  $g + 4 = 0.7h$



2) Allie has collected some data on students' heights as they age. Which category would be the dependent variable? Which would be the independent variable?

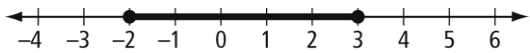
### 6.3 Warm-Up

1. Describe in words the values represented by the number line.



2. Draw a number line to represent all numbers that are less than  $-2$ .

3. Describe in words the values represented by the number line.



4. Draw a number line that represents all numbers that are greater than 4 and less than or equal to 7.

5. A car travels at 60 km/h for 5 h. Suppose you were to create a graph of this scenario.

a) What scale would you use along the time axis? What value would you start at? What value would you end at?

b) What scale would you use along the distance axis? What value would you start at? What value would you end at?