

The Natural Logarithm

The inverse of $y = e^x$ would be the logarithmic function $y = \log_e x$. Because of the significance of e in representing the idea of instantaneous growth, $\log_e x$ became known as the **natural logarithm** of x and was defined as $\ln x$. This is read as the natural log of x , log base e of x , or more simply “lawn” x .

Alternately, $\log_e x = \ln x$

Thus $\ln 1 = 0$ because $e^0 = 1$ and $\ln e^4 = 4$ because $e^4 = e^4$.

$\ln e^4 = "x"$
 $e^x = e^4$
 $x = 4$

$\ln 0$ is undefined because e^0 must be greater than 0

$\ln 2 = 0.693$ because $e^{.693} = 2$

$e^{\ln 2} = 2$ $e^{\ln 10} = 10$ $e^{\ln e} = e$ $e^{\ln x} = x$

For those of you who felt a math joke coming, here it is (**WARNING** This joke may be offensive to some)

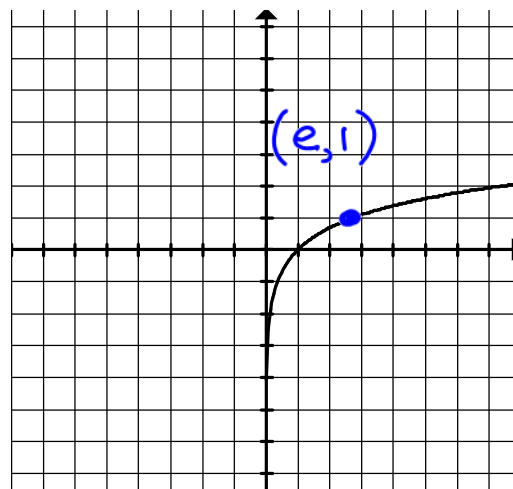
Question: What is the number one name in the world?

Answer: Lonnie ($\ln e$)

$\ln e = 1$

The graph of $y = \ln x$ should behave in a similar way to the graph of $y = \log x$

x-int at (1,0)
 asymptote at $x=0$
 no y-intercept.



Something to ponder: The equation $e^{i\pi} + 1 = 0$ is considered by many mathematicians to be among the most “beautiful” in all of mathematics. It nicely relates probably the 5 most important numbers in all of mathematics: 1, 0, e , π , and $i(\sqrt{-1})$